# Implementation of Artificial Communication Channel for Motor Patients

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*Abstract*: Brain Computer Interface establishes a direct communication pathway between human brain and outside world. This capability of Brain Computer Interface system enables patients suffering from severe motor disorder or complete body paralysis to control variety of applications like, controlling a cursor on computer screen, controlling the movement of a robotic or a wheel arm chair and many more. The efficiency of a Brain Computer Interface system completely rely on efficient pre-processing and classification algorithms. In present work, a methodology of feature extraction and classification of Electroencephalogram signals is proposed for implementation of Brain Computer Interface for physically disabled. The EEG signal under consideration has been recorded from seven different subjects performing five different mental tasks. Time Frequency Energy Distribution spectrum is computed from the coefficient obtained from Hilbert Huang transform of Electroencephalogram signals. Four statistical parameters are calculated from the TFED of signals as features. For classification, Support Vector Machine classifier model is employed. The results of the classification show efficacy of present methodology of feature extraction and classification for implementation of Brain Computer Interface.

*Index Terms*: Brain Computer Interface (BCI), Electroencephalogram (EEG), Hilbert Huang Transform (HHT), Support Vector Machine (SVM), Classification

#### I. INTRODUCTION

Electrical activity of human brain for different metal states and corresponding for reality or imagination can be efficiently recorded simply by placing electrodes on human scalp. Recording of the electrical signals is called Electroencephalograph which in turn is useful to establish an artificial man machine interface (MMI) or Brain Computer Interface (BCI). A Brain Computer Interface (BCI) is an alternate pathway for communication between human brain and the outside world. BCI capabilities are largely helpful to the patient suffering from severe motor disorder to communicate and control assistive appliances and applications using brain power [1]. A BCI permits an individual with severe motor disabilities to achieve a good control to an external device via the thoughts and works as new mode of human-computer interaction. It also works as a significant diagnostic tool that facilitated the study and analysis of brain abnormalities.

Major breakthrough in the field of BCI research was marked after invention of non-invasive techniques for Electroencephalogram (EEG) signals recording. Previously, electrodes and sensors were implanted inside the brain using invasive techniques. EEG signals recorded by using invasive techniques are less noisy due to less contamination from surroundings. But, user has to go under surgery for implantation [2]. This makes invasive techniques an expensive and cumbersome approach. Various patterns of rhythmic or periodic activity exhibit by EEG signals can be divided in the frequency bands likewise 0.1- 3.5Hz (delta), 4-7.5Hz (theta), 8-13Hz (alpha), 13-30Hz (beta) and >30Hz (gamma) [3-4]. In this work, we have used EEG signals, recorded using non-invasive methods only. The essential steps for BCI realization are recording of brain electrical activity, pre-processing, feature extraction, classification and finally command generation. Successful working of a BCI is determined by careful measures taken during each step. Pre-processing the EEG signals combines filtration and noise removal from raw EEG data. Signals recorded using noninvasive techniques are more prone to noise. Common Spatial Pattern (CSP), Independent Component Analysis (ICA), Principle Component Analysis (PCA) and Multi scale PCA (MSPCA) are very common and mostly used algorithms for EEG signals processing [5]. MSPCA has been applied on different biomedical signals and images for pre-processing and de-noising, like Sharma et al. [6] have proposed MSPCA for denoising multichannel Electrocardiogram (ECG) signals. Zhang and Zhang [7] employed Gabor Wavelet based MSPCA and SVM for face recognition. Many researchers have also applied MSPCA model for analyzing and pre-processing EEG data. Neuromechanism employed for EEG signals recording affects largely the efficiency of BCI in terms of time and classification. Most commonly used neuromechanism are sensorimotor activity [9-11], Visual Evoked Potential (VEP) [12], Slow Cortical Potential (SCP) [13] and P300. EEG signals employed in present work are recorded for imagined motor activity using sensorimotor activity as neuromechanism for left fist blink, right blink and both leg movement.

It is evident from the previous studies that EEG signal are non-stationary in nature [14]. Hence, the EEG signal processing techniques should consider non-stationary characteristics of EEG signals effectively. Among various non-stationary techniques available, the Hilbert Huang Transform (HHT) technique has been extensively used in recent years for non-stationary signal analysis in diverse domains such as in speech signal processing [15], biomedical engineering [16] and fault feature identification [17].

In present work, EEG signals recorded for five different mental tasks are i.e. baseline tasks, figure rotation task, letter composition task, Maths task and visual counting task are considered for BCI implementation. Firstly, signals are passed through MSPCA model for reconstructing simplified EEG signals. Further, HHT based method is applied for the successful implementation of the BCI.

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Empirical Mode Decomposition (EMD) is performed on EEG signals to obtain series of mono-component modes with local characteristic time scales called Intrinsic Mode Functions (IMF). Further, Instantaneous Frequency of each IMF was represented through Hilbert transform. The methodology proposed in present work is useful for extracting features, classifying mental task based EEG data using extracted features, and generating command with higher classification efficiency. EEG signal shows different classification performance for different set of subjects. Proposed methodology is used for analyzing feasibility of EEG signals recorded corresponding to different mental tasks, for higher classification efficiency. Fig.1 shows overall methodology presented in this work.



Fig. 1 Methodology proposed for EEG signals feature extraction and classification

# II. EEG DATABASE

The EEG database used in present study is taken from Keirn and Aunon study [18]. The subjects were seated in a sound controlled compartment with shadowy environment and noise-less ventilation. To record EEG signals, elastic electrode were used and placed at the six different positions on scalp viz. C3, C4, P3, P4, O1 and O2. The electrodes were place as per the international 10 -20 system of electrode placement [19]. However, the reference is taken as A1 and A2 to electrically linked mastoids. The electrodes are connected through a bank of amplifiers (Grass7P511), whose band-pass analog filters are set at 0.1 to100 Hz. The data are sampled at 250 Hz with a Lab Master 12-bit A/D converter mounted on a computer. Signals are recorded for 10 sec during one trial and each task is performed for generating 10 such trials. In this paper, EEG signals from seven subjects performing five different mental tasks are considered for analysis. The five mental tasks are described as follows:

**1. Baseline task:** The subjects were asked to relax without any thinking in mind in particular. This task is used as a reference and as a baseline measure of the EEG signals.

2. Math task: The subjects were asked to solve multiplication problems, such as 13 times 17 without vocalizing or making any other physical overt movements. The tasks are non-repeating and difficult so that an immediate answer is not obvious. The subjects verified at the end of the task for the solution. It was ensured that no subject completed the task before the 10s duration recording time.

**3.** Figure rotation task: The subjects were given to observe the drawing of a three dimensional block object, after which the drawing was removed and the subjects were asked to visualize the object being rotated about an axis.

4. Letter task: The subjects were asked to mentally compose a letter to a person without vocalizing. The task was repeated several times and the subjects was asked to continue with the letter from where they left off in the next period.

5. Visual counting task: The subjects were asked to imagine a blackboard and to visualize numbers being written on the board sequentially, with the previous number being erased before the next number was written. The subjects were instructed not to verbalize the numbers but to visualize them.

## III. OVERVIEW OF TECHNIQUES

#### 3.1 MULTISCALE PCA

When the behavior of the events associated with various phenomenon changes rapidly with time and frequency, MSPCA is found to be suitable modelling technique. The modelling of single scale data can be efficiently performed by PCA alone, as algorithm considers relationship of data for same time-frequency localization. However all practical data sources generate data which is multiscale in nature. Hence, it is feasible to use PCA with multiscale capabilities. MSPCA performs computation of PCA on wavelet coefficients at each scale and combines results at significant scales [20]. In MSPCA algorithm, first the data is decomposed in time-frequency using certain wavelets. Then the PCA is applied for the coefficients of each scale irrelevant to one another. Combination of the models corresponding to important scales takes place to obtain a unified model [20].

In present work, we have applied MSPCA to simplify the EEG data matrix. For decomposition of EEG data, Symlets wavelet is selected and decomposition level was set to 5. However, Kaiser's rule is followed for retaining Principle Components (PCs). According to Kaiser's rule, only those components are retained which are having Eigen values (Variance) greater than the mean of all Eigen values. Fig.2 (a-b) shows the EEG data plots (in  $\mu$ V) before applying MSPCA and after application of MSPCA.





#### **3.2 SUPPORT VECTOR MACHINE**

SVM is the statistical learning classification algorithm, which can be applied for classification of two or multi classes of data. SVM model was developed by Vapnik in 1995 [21]. SVM is being used by many researchers because of its attractive features such as Empirical Risk Minimisation (ERM) principle and Structural Risk Minimisation (SRM) principle. This makes SVM a strong classification tool [22]. In SVM a hyperplane is created which maintains a large gap between the two classes of data. Support Vectors are closest point to this hyperplane and SVM model ensures maximum gap for closest support vectors of both the classes from hyperplane [23].

Let data set be (*xi*, *yi*), with *L* training points, where each input *xi* has *D* attributes, and belongs only one of two classes yi = -1 or +1. If *w* is normal to the hyperplane and *b/w* is perpendicular distance from the hyperplane to the origin, expression for hyperplane can be written as:

$$w * x + b = 0 \tag{1}$$

Fig.3 represents hyperplane, separating two linearly separable classes. *L1* and *L2* is the maximum distance of support vectors from hyperplane.

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Fig. 3 Hyperplane separating two classes of data.

#### 3.3 Hilbert Huang Transform (HHT)

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It is an effective tool for the analysis of nonlinear and non-stationary signals. It provides a good description of local oscillating frequency components present in the signal. HHT is the combination two basic steps: Empirical Mode Decomposition (EMD) and Hilbert Spectral Analysis.

#### 3.3.1 Empirical Mode Decomposition (EMD)

If we consider any arbitrary signal as composed of a series of different intrinsic oscillation modes, then the EMD [24] can be used for decomposition the incoming signals into its different Intrinsic Mode Functions (IMF). The algorithm of generating IMFs is given in the following steps:

Step1: Determine the local extremes (maxima and minima) of the signal x(t).

Step2: Generate the lower envelope el(t) and upper envelope em(t) by connecting all local minima and local maxima respectively using spline interpolation function.

Step3: Determine the local mean as m(t = (el(t) + em(t))/2.

Step4: Subtract the local mean from the signal, hi(t)=x(t)-m(t).

Step5: Check whether hi(t) is an IMF or not by checking the basic conditions mentioned above. If h(t) satisfies the criteria, then set IMFi = hi(t), and assign ci(t) = IMFi(t). Else x(t)=hi(t) and repeat steps 1-4.

Step6: To determine rest of IMFs, let ri(t)=x(t)-IMFi. Repeat the steps 1-5 assuming ri(t) as new x(t) until ri(t) becomes a monotonic residual signal. At the end of the decomposition, x(t) can be written as: X (t) =  $\sum_{n=1}^{M} c_n + r_M$ 

Where, N is the number of intrinsic mode functions, cn(t) is the  $n^{th}$  IMF and rm(t) is the final residual monotonic function.

However, an IMF is a function that satisfies following two conditions:

1. In the entire signal, the number of extremes and the zero-crossings must be equal or differ at most by one.

2. At any point, the mean value of the envelope defined by the local maxima and the envelope defined by the local minima must be zero.

#### 3.3.2 Hilbert spectral analysis

IMFs generated using EMD generates signals which contain one frequency component at one time. Further, Hilbert transform is applied on every IMF obtained by EMD to compute IFs. Hilbert transform cannot be directly applied on the non-stationary and nonlinear signal which are having more than one frequency component at a given time. For signal x(t) of Lp class [25], Hilbert transform is:

$$Y(t) = \frac{1}{\pi} PV \int_{-\infty}^{\infty} \frac{x(\tau)}{(t-\tau)} d\tau$$

Where, PV denotes the Cauchy's principle integral value. Using this, analytic function Z(t) can be computed as:

 $Z(t) = x(t) + j \cdot y(t) = a(t)e^{j\phi(t)}$ 

Computation of instantaneous frequencies can be given as below.

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$$F(t) = \frac{1}{2\pi} \frac{d\phi(t)}{dt}$$

3.4 Time frequency energy distribution (TFED)

The Time-Frequency–Energy Distribution (TFED) can represent the characteristics of signal in both time and frequency domains. More subtle features can be obtained from TFED [26, 27]. It is much better than the traditional approaches like Short-Time Fourier Transform (STFT), Wigner–Ville, Choi–Williams Distribution [28]. As, these transforms are not able to decompose the signals adaptively and are also constrained by the uncertain principle which results in the confliction between time resolution and frequency resolution [28, 29]. The Hilbert spectrum is calculated as:

$$H(w,t) = Re(\sum_{i=1}^{n} a_i(t)e^{j\int Wi(t)dt})$$

The Hilbert Spectrum (HS) represents the TFED. The overall HS is expressed as the superposition of the individual IMFs" HSs defined as:  $H(k,t) = \sum_{i=1}^{b} (k,t); b=1, 2, \dots, B.$ 

Hence, each element H(k,t) of HS is defined as the weighted sum of the instantaneous amplitudes of all the IMFs at  $k^{th}$  frequency bin.

#### IV. BCI IMPLEMENTATION 4.1 FEATURE EXTRACTION AND CLASSIFICATION

HHT based features are extracted from preprocessed EEG signals and feature vector is prepared to train classifier. The feature extraction is carried out in three steps. In the first step, HHT is performed. Which is followed by the calculation of Time-Frequency Energy Distribution (TFED) also known as Hilbert spectrum, in the second

step. HHT is a self-adaptive signal analysis method. The Hilbert Spectrum based on HHT offers amplitude distribution with the change of time and frequency i.e. it provides a complete TFED which is more accurate than the other time– frequency analysis methods including wavelets [30-32]. Therefore, it is suitable to obtain the TFED of a signal using HHT. At last, the estimation of time-frequency parameters is applied for feature extraction. In this work, four statistical parameters i.e. **Mean**, **Standard Deviation**, **Skewness** and **Variance** have been computed from Hilbert spectrum to prepare the final feature vectors.

In present work, SVM classifier is employed for classification or identification of the class of EEG signals. Once the SVM classifier is trained, it can be used for recognition of EEG signals and consecutively generate the external command. The generated external command can be used for controlling various assistive devices and applications.

## V. RESULTS

Statistical features obtained from Hilbert spectrum of calculated of brain signals recorded during performing five different mental tasks are used to prepare input feature vector for training and validation of classification algorithm SVM. The signals have been recorded from seven different subjects while performing five tasks in certain number of trials to attain a better accuracy. The IMFs of EEG signal corresponding to each task has been computed. After that, IF vectors has been computed for each IMFs using Hilbert transform which is further used to calculate the Hilbert spectrum and statistical features. The feature vectors are passed through the SVM classifier to have high accuracy. The confusion matrix prepared using the SVM is prepared for all the five tasks for each seven subjects. Table 1-7 shows the confusion matrix prepared for the tasks for subject 1 to subject 7 respectively. Table 8 represents the classification accuracy obtained after considering only two tasks (out of five tasks) at a time, for all the seven subjects.

 Table (1) Confusion matrix for Subject-1

BAS	COU	LET	MUL	ROT	CLASSIFIED AS
66	0	3	1	1	Baseline (BASE)
0	67	1	0	3	Counting (COU)
2	3	64	1	1	Letter (LET)
0	0	0	71	0	Multiplication (MUL)
1	1	1	0	68	Rotation (ROT)

Table (2) Confusion matrix for Subject-2

BAS	COU	LET	MUL	ROT	CLASSIFIED AS
35	0	0	1	0	Baseline (BASE)
0	24	9	0	3	Counting (COU)
0	10	21	1	4	Letter (LET)
1	1	0	32	1	Multiplication (MUL)
0	6	6	1	16	Rotation (ROT)

Table (3) Confusion matrix for Subject-3

BAS	COU	LET	MUL	ROT	CLASSIFIED AS
67	2	1	0	1	Baseline (BASE)
1	64	5	0	1	Counting (COU)
1	2	61	2	4	Letter (LET)
0	0	2	69	0	Multiplication (MUL)
1	2	6	1	61	Rotation (ROT)

 Table (4) Confusion matrix for Subject-4

	BAS	COU	LET	MUL	ROT	CLASSIFIED AS
	65	1	4	0	1	Baseline (BASE)
	0	70	1	0	0	Counting (COU)
	1	3	66	1	0	Letter (LET)
	2	0	0	67	2	Multiplication (MUL)
[	4	0	0	8	52	Rotation (ROT)

Table (5) Confusion matrix for Subject-5

BAS	COU	LET	MUL	ROT	CLASSIFIED AS
67	1	1	2	0	Baseline (BASE)
1	69	1	00	0	Counting (COU)
0	0	68	2	1	Letter (LET)
2	0	1	67	1	Multiplication (MUL)
0	0	0	1	70	Rotation (ROT)

Table (6) Confusion matrix for Subject-6

BAS	COU	LET	MUL	ROT	CLASSIFIED AS
60	3	4	1	3	Baseline (BASE)
4	61	3	3	0	Counting (COU)
7	1	56	б	1	Letter (LET)
2	1	5	67	1	Multiplication (MUL)
1	1	0	0	69	Rotation (ROT)

BAS	COU	LET	MUL	ROT	CLASSIFIED AS
31	2	0	2	1	Baseline (BASE)
4	27	3	2	0	Counting (COU)
0	7	26	3	0	Letter (LET)
1	2	1	30	2	Multiplication (MUL)
10	0	0	1	34	Rotation (ROT)

 Table (7) Confusion matrix for Subject-7

Table (8) Classification accuracy for one-versus-one mental tasks for all seven subjects using SVM classifier

TASKS	<b>S1</b>	S2	<b>S</b> 3	S4	<b>S</b> 5	S6	S7
BAS_CON	97.90	100	97.19	98.57	97.19	89.26	94.33
BAS_LET	97.90	100	97.90	96.99	97.19	87.88	94.33
BAS_MUL	98.62	100	97.19	96.42	94.33	93.55	90.10
BAS_ROT	98.62	97.19	98.63	98.57	98.62	92.88	95.75
COU_LET	96.47	65.76	90.76	98.49	98.62	92.19	77.14
COU_MUL	100	76.25	98.62	96.42	100	96.44	84.33
COU_ROT	97.19	100	96.48	97.14	100	96.47	100
LET_MUL	98.62	74.63	96.47	98.49	97.90	92.19	88.62
LET_ROT	97.90	95.76	92.19	91.72	97.90	95	88.62
MUL_ROT	100	96.87	97.90	94.28	97.90	97.90	91.46
All tasks	94.62	73.84	90.90	91.83	96%	86.62	81.76

The classification results obtained with the methodology presented in this paper are shown in Table 1-8. The classification accuracy has been calculated considering two certain tasks at a time. In this way, all relative classification accuracy between every two tasks has been compared. Finally, an average accuracy has been calculated considering all the tasks at a time and shown in Table 8. It can be perceived from Table 8 that the classification accuracies for the most of the tasks combinations is greater than 80%, with many task combinations having a classification accuracy of 100%.

## VI. CONCLUSION

In this work a feature extraction method is proposed for the processing of EEG signals recorded for performing mental tasks and classification of those mental tasks. The proposed methodology helps in successful implementation of the Brain Computer Communication channel. It is based on the HHT and the estimation of statistical parameters such as standard deviation, variance, mean and skewness for Hilbert spectrum. The efficacy of the present methodology can be confirmed by the high classification accuracy for one-versus-one mental task classification using a simple SVM classifier. The average classification accuracy obtained is around above than 90%. So, This work suggests a simple feature extraction technique, which can be effectively used for the implementation of the Brain Computer Communication channel for controlling assistive devices and the assistive applications.

#### REFERENCES

1. J.M. Iturrate, A. Antelis, J. Kubler, and Minguez, "A non-invasive brain actuated wheelchair based on a P300 neurophysiological protocol and automated navigation," IEEE Transactions on Robotics, vol. 25, pp. 614-627, 2009

2. R. Upadhyay, P.K. Kankar, P.K. Padhy and V.K. Gupta "Robot motion control using brain computer interface", IEEE conference on control, automation, robotics and embedded systems, 2013.

3. S. Kelly, D. Burke, P.D. Chazal, and R. Reilly, "Parametric models and spectral analysis for classification in Brain-Computer Interfaces," 14th International Conference on Digital Signal Processing, vol. 1, pp. 307 – 310, 2002.

4. R. Upadhyay, P.K. Kankar, P.K. Padhy, and V.K. Gupta, "Extraction and Classification of Electroencephalogram signals," IEEE International Conference on Computational Intelligence and Computing Research, pp. 1-4, 2012.

5. R. Upadhyay, A. Manglick, D.K. Reddy, P.K. Padhy and P.K. Kankar, "Channel optimization and nonlinear feature extraction for Electroencephalogram signals classification", Computers and Electrical Engineering, 2015; 45: 222–234.

Sharma, L. N., Dandapat, L. N. and Mahanta, A. (2010), Multiscale Principal Component Analysis to Denoise
 ECG Signals", IEEE 5<sup>th</sup> Cairo International Biomedical Engineering Conference, pp.17-20.

8. Zhang, G. and Zhang, J. (2008) "Face Recognition Using Multi-Scale PCA and Support Vector Machine", 7<sup>th</sup> World Congress on Intelligent Control and Automation, pp. 5906-5910.

9. Xie, S. and Krishnan, S. (2011) "Signal Decomposition by Multi-scale PCA and Its Application to Long-term EEG Signal Classification", IEEE/ICME International Conference on Complex Medical Engineering, pp. 532-537.

10. G. Pfurtscheller, and A. Aranibar, "Event-related cortical desynchronization detected by power measurements of scalp EEG," Electroencephalogr. Clin. Neurophysiol., vol. 42, pp. 817–26, 1977.

11. H. Jasper, and W. Penfield, "Electrocortiograms in man: effect of voluntary movement upon the electrical activity of the precentral gyrus," Arch. Psychiat. Nervenkr., vol. 183, pp. 163–74, 1949.

12. H. Ramoser, J.M. Gerking, and G. Pfurtscheller, "Optimal spatial filtering of single trial eeg during imagined hand movement," Rehabilitation Engineering, IEEE Transactions on Neural Systems and Rehabilitation, vol. 8, pp. 441-446, 2000.

13. Kubler, B. Kotchoubey, J. Kaiser, J.R. Wolpaw, and N. Birbaumer, "Brain-computer communication: unlocking the locked," Psychol. Bull., vol. 127, pp. 358–75, 2001.

14. N. Neumann, A. Kubler, J. Kaiser, T. Hinterberger, and N. Birbaumer, "Conscious perception of brain states: Mental strategies for brain–computer communication," Neuropsychologia, vol. 41, pp. 1028–36, 2003.

15. C.W. Anderson and J. A. Bratman, "Translating Thoughts Into Actions by Finding Patterns in Brainwave", Fourteenth Yale Workshop on Adaptive and Learning Systems, Yale University, New Haven, CT, USA, June 2008, pp. 1-6

16. H. Huang, J. Pan, Speech pitch determination based on Hilbert– Huang transform, SignalProcess. 86(4)(2006)792–803.

17. H. Liang, H. L. Qiu, J. D. Z. Chen, Application of the empirical mode decomposition to the analysis of esophageal manometric data in gastroesophagealrefluxdisease,IEEETrans.Biomed.Eng.52(10) (2005)1692–1701.

18. N. Roveri, A. Carcaterra, Damage detection in structures under traveling oads by Hilbert– Huang transform, Mech. Syst. Signal Process. 28(2012)128–144.

19. Keirn, Z.A., and Aunon, J.I., "A new mode of communication between man and his surroundings," IEEE Transactions on Biomedical Engineering, vol. 37, no.12, pp. 1209-1214, December 1990.

20. D.G. Domenick, "International 10-20 Electrode Placement System for Sleep", 1998. http://members.aol.com/aduial/1020sys.html.

21. B.R. Bakshi, "Multiscale PCA with Application to Multivariate Statistical Process Monitoring," AIChE Journal, 1998.

22. C. Cortes and V. Vapnik, Support vector networks. Machine Learning, vol. 20, pp. 273--297, 1995.

23. S. R. Gunn, Support Vector Machines for Classification and Regression, 1998

24. T. Fletcher, Support Vector Machines Explained, unpublished.

25. N. E. Huang, Z. Shen, S. R. Long, M. L.Wu, H. H. Shih, Q. Zheng, N. C.Yen, C. C. Tung, and H. H. Liu, "The empirical mode decomposition and Hilbert spectrum for nonlinear and nonstationary time series analysis," Proc. R. Soc. London A, vol. 454, pp. 903–995,1998

26. F.W. Byron, R.W. Fuller, Mathematics of Classical and Quantum Physics, Dover Publications, Inc., New York, 1992.

27. Li, L., Ji, H.B., Jiang, L.: "Quadratic time-frequency analysis and sequential recognition for specific emitter identification", IET Signal Process. 2011, 5, (6), pp. 568-574

28. Chen, T.C.: "Joint signal parameter estimation of frequency hopping communications", IET Commun., 2012, 6, (4), pp. 381–389

29. Karlsson, S., Yu, J., Akay, M.: "Time-frequency analysis of myoelectric signals during dynamic contractions: a comparative study", IEEE Trans. Biomed. Eng., 2000, 47, (2), pp. 228–238

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30. Zhao, Z.D., Zhao, Z.J., Chen, Y.Q.: "Time-frequency analysis of heart sound based on HHT". 2005 Int. Conf. on Communications, Circuits and Systems, 2005, pp. 926–929.

31. Song, C.Y., Xu, J.M., Zhan, Y.: "A method for specific emitter identification based on empirical mode decomposition". 2010 IEEE Int. Conf. on Wireless Communications, Networking and Information Security (WCNIS), Beijing, China, June 2010, pp. 54–57

32. Huang, N.E., Shen, Z., Long, S.R.: "The empirical mode decomposition and the Hilbert spectrum for nonlinear and non-stationary – time series analysis, Proc. R. Soc. Lond. A, 1998, 454, (1997), pp. 903–995

33. Correa, T.K., Asce, A.M., Kareem, A., et al.: "Efficacy of Hilbert and wavelet transforms for time– frequency analysis", J. Eng. Mech., 2006, 132, (10), pp. 1037–1049

